

# Multi-Agent Formation Control

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For Implementation of Group Strategies

Aubrey Hormel  
Mentor: Dr. Jingjin Yu

# Problem Formulation

# Initial and Goal Positions in Multi-Robot System

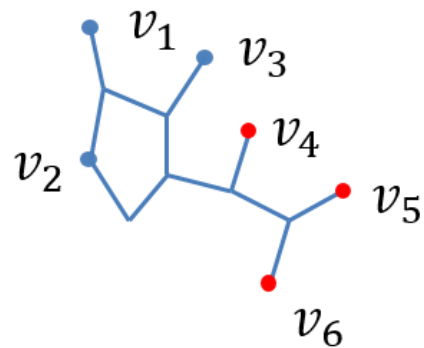
Agents move from initial to target nodes by travelling along edges in a connected graph.

Constraints:

- Optimize total distance travelled by all agents
- Avoid collision

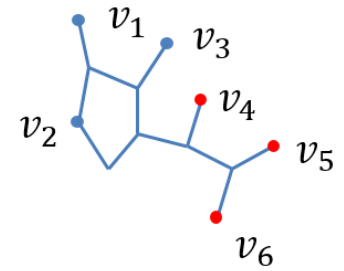
Allowances:

- Agents are indistinguishable - a given agent is allowed to be mapped to any goal node



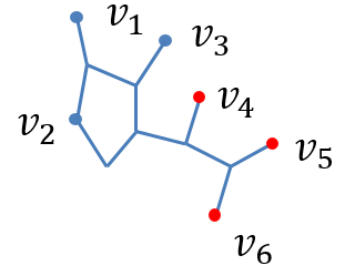
# Distance-Optimal Pairing

Perform a Breadth-First Search (BFS) to construct a distance matrix between each initial/goal node pair.



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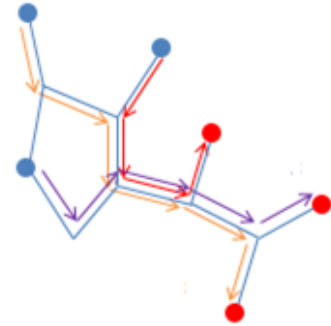


Perform Hungarian Algorithm to find optimal pairing

	$v_4$	$v_5$	$v_6$
$v_1$	5	6	6
$v_2$	4	5	5
$v_3$	4	5	5

# Path Planning

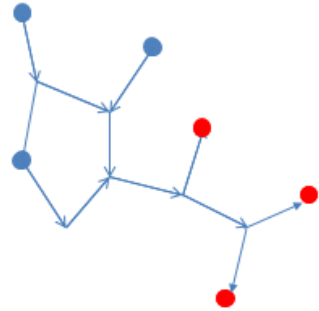
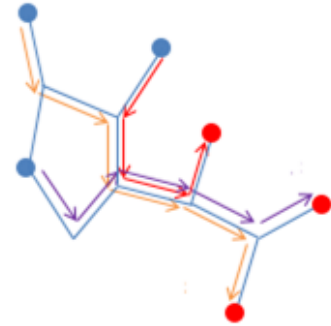
Creates a shortest- yet unscheduled- path set



# Path Planning

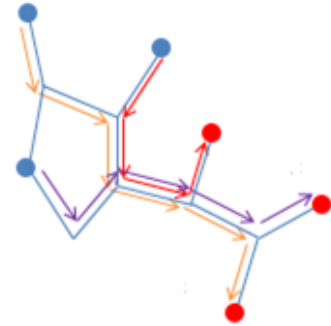
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Path set induces a directed acyclic graph (DAG)

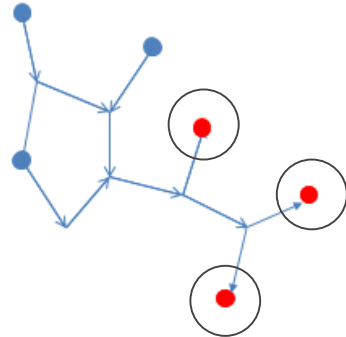


# Path Planning

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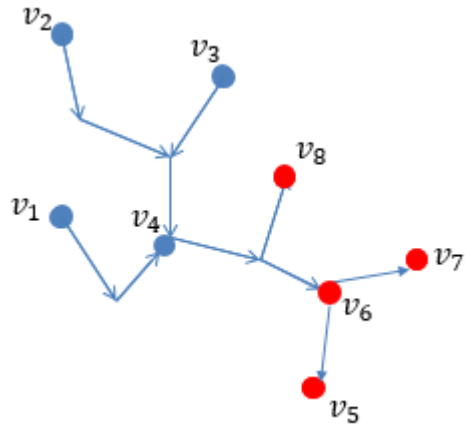
Identify **standalone** goal nodes- those goal nodes which lie in only one path.

Given priority in scheduling algorithm



# Path Scheduling Process

# Path Scheduling

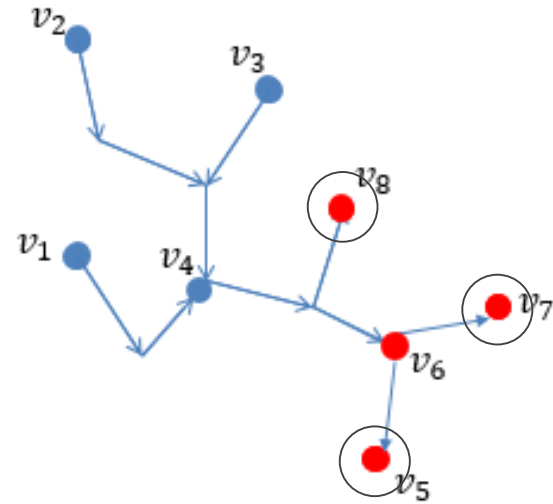


	$v_5$	$v_6$	$v_7$	$v_8$
$v_1$	5	4	5	4
$v_2$	6	5	6	5
$v_3$	5	4	5	4
$v_4$	3	2	3	2

# Path Scheduling

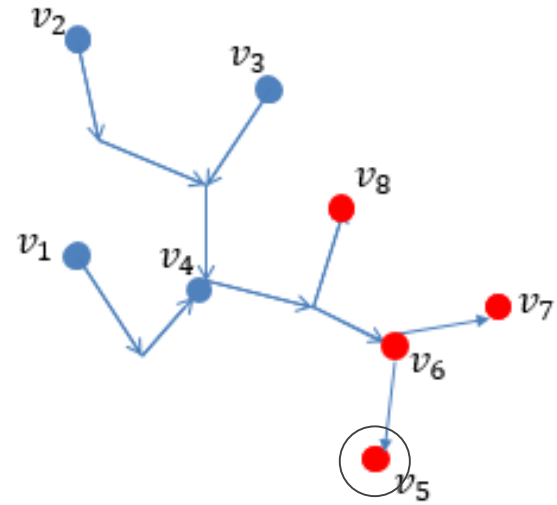
Identify standalone goal nodes

Standalones:  $\{v_5, v_7, v_8\}$



# Path Scheduling

WLOG, choose a standalone goal node to schedule an agent to.

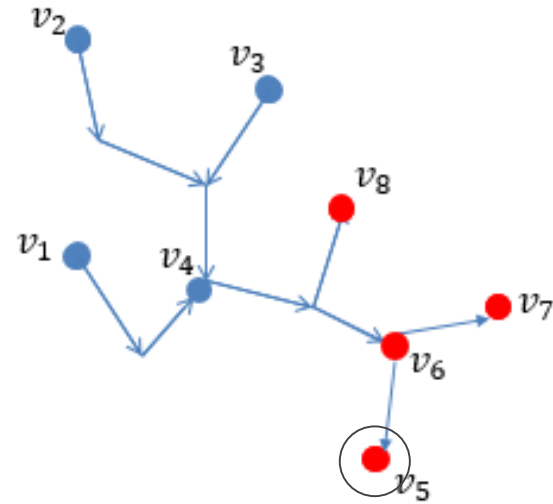


# Path Scheduling

Recall:

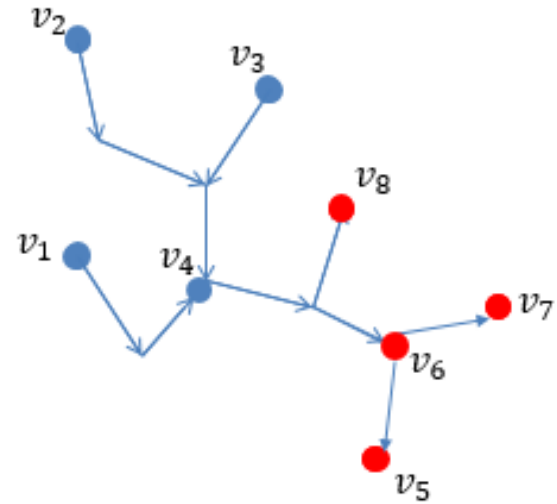
Hungarian Algorithm paired  $v_1$  with  $v_5$

	$v_5$	$v_6$	$v_7$	$v_8$
$v_1$	5	4	5	4
$v_2$	6	5	6	5
$v_3$	5	4	5	4
$v_4$	3	2	3	2



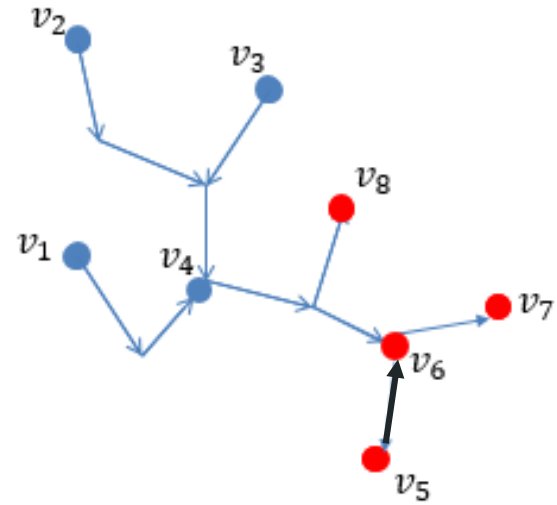
# Path Scheduling

Perform “reverse” BFS on directed edges until first initial node is found.



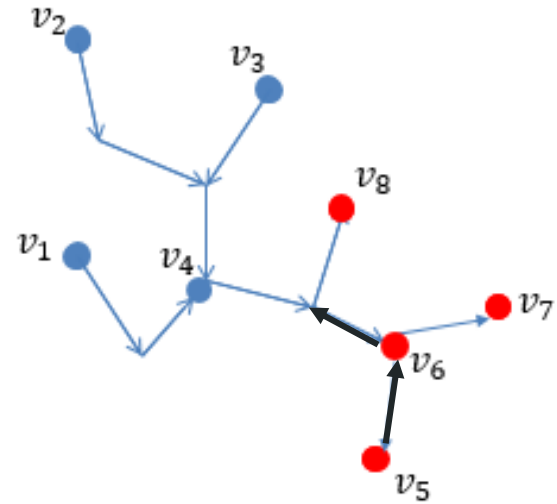
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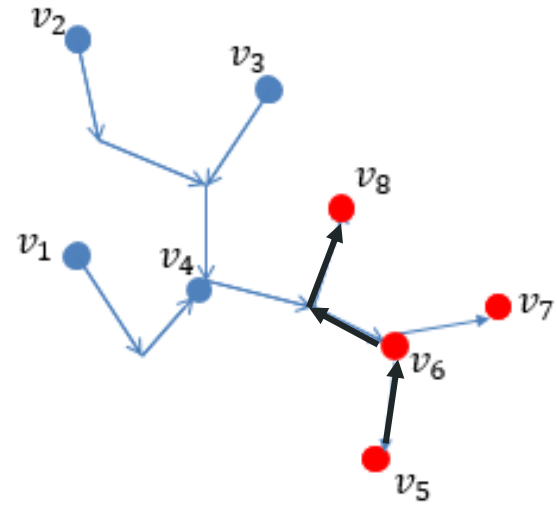
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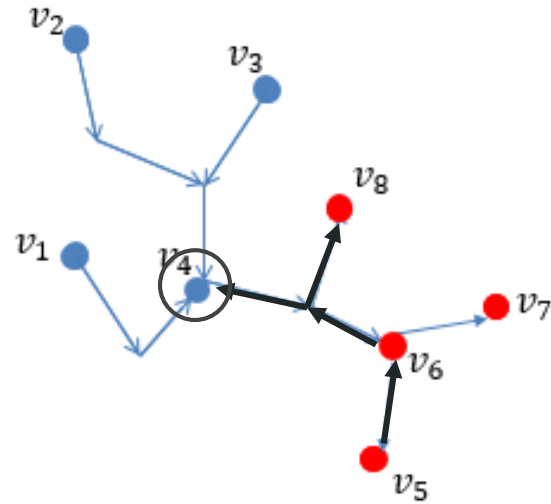
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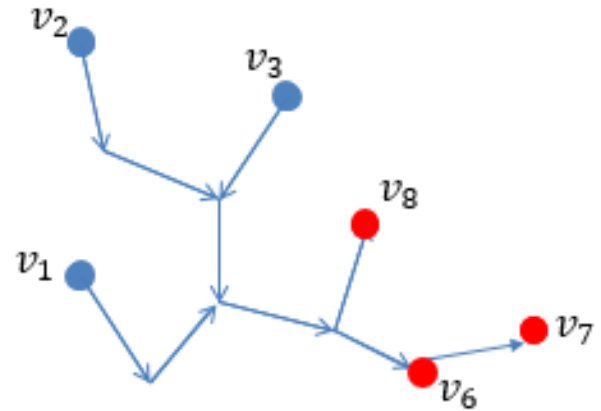
Agent present at  $v_4$  is then assigned to move to  $v_5$  and given start time  $t = 0$



# Path Scheduling

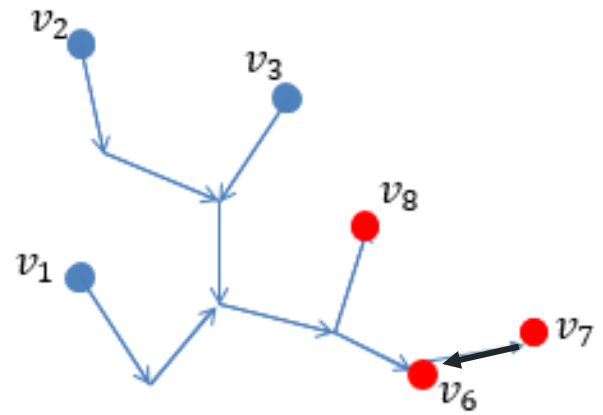
Prune the DAG so that the previously scheduled initial and goal nodes are now ignored.

Updated set of standalone goal nodes:  
 $\{v_7, v_8\}$



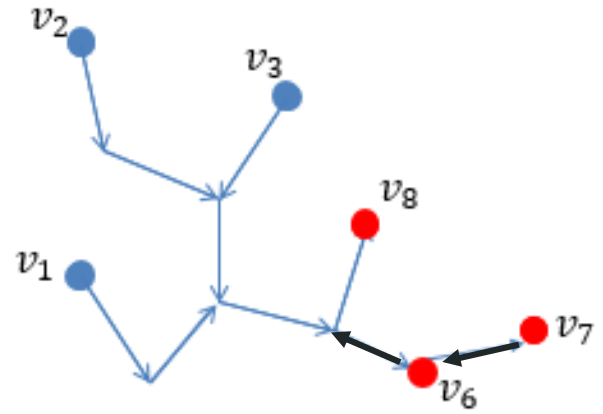
# Path Scheduling

Let's do it again!



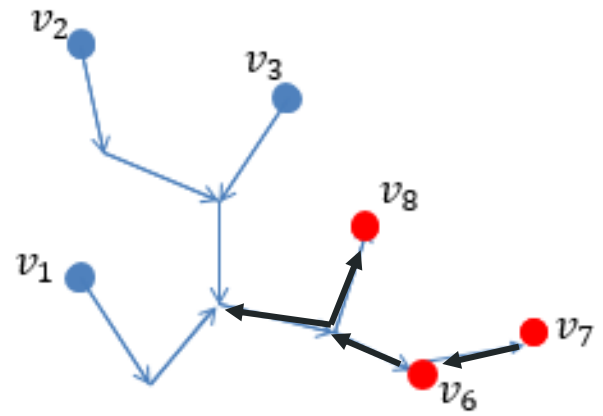
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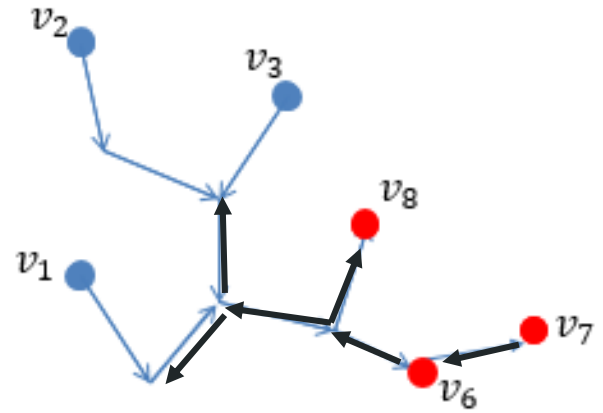
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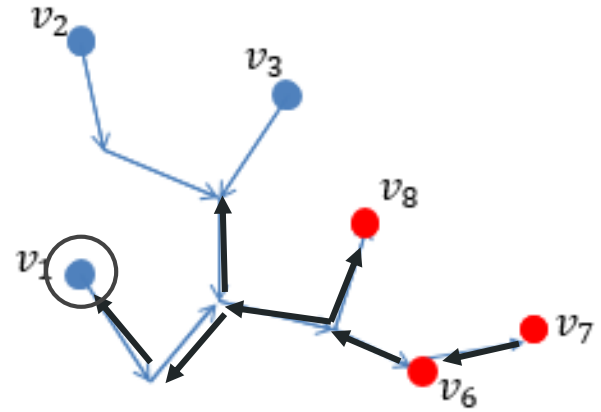
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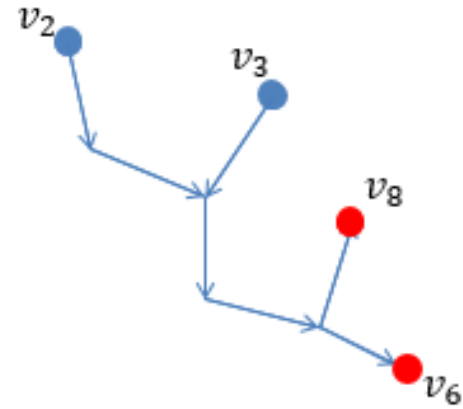
Agent at  $v_1$  moves to  $v_7$  and is assigned start time  $t = 1$



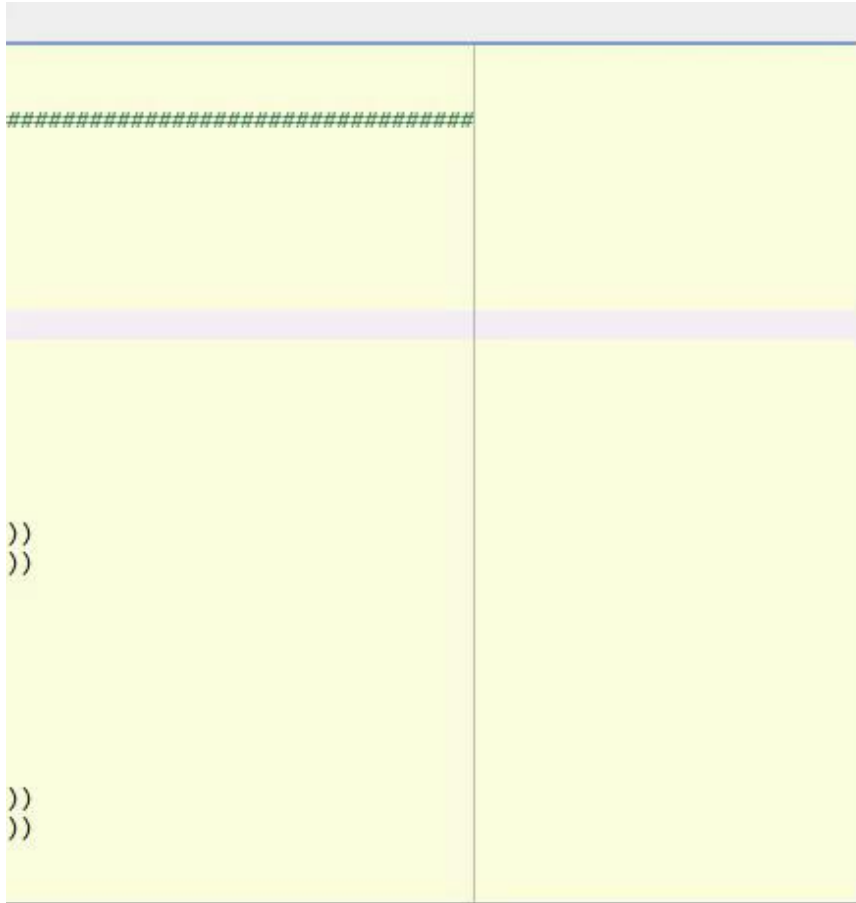


# Path Scheduling

Updated standalone goal nodes:  $\{v_6, v_8\}$



# Simulations



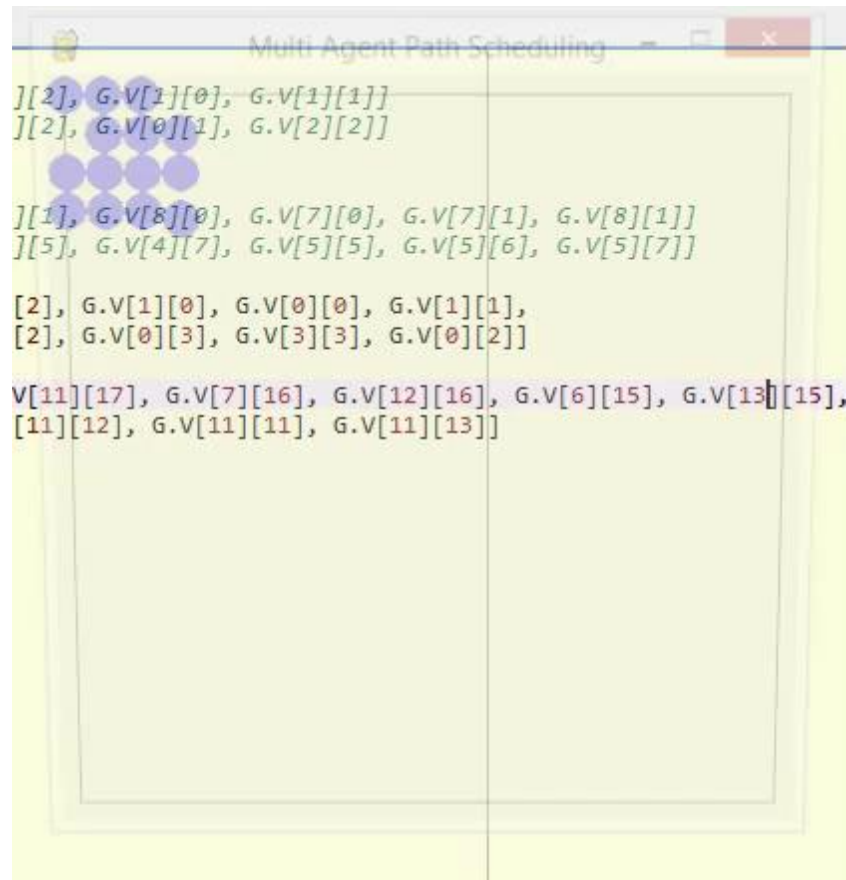
Multi Agent Path Scheduling

is is run through all vertices in  $V$  and add to adj list if dist = 1  
graph)  
t way to do this

```
.coords[0] < self.bounds[0]:  
    and v.coords[1] < self.bounds[1]:  
        )
```

ng down first on the BFS - makes it more likely for them to utilize the abundan

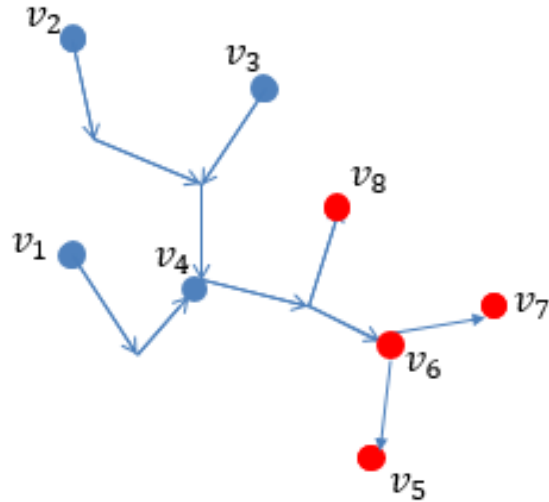
The diagram shows a 10x10 grid. The top two rows (rows 1 and 2) contain blue circular nodes. The bottom three rows (rows 7, 8, and 9) contain red circular nodes with a plus sign inside. A horizontal purple bar highlights the middle section of the grid (rows 4, 5, and 6).



# Room for Improvement

# Current Issues

- It is not necessary to assign each agent a different start time.



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- Some randomly generated initial and goal formations break my algorithm for pruning the DAG.

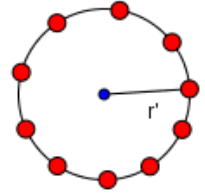
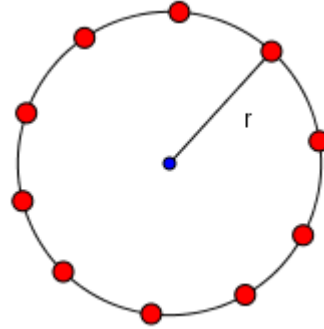


# Current Issues

- It is not necessary to assign each agent a different start time.
- Some randomly generated initial and goal formations break my algorithm for pruning the DAG.
  - But- I have some ideas :)

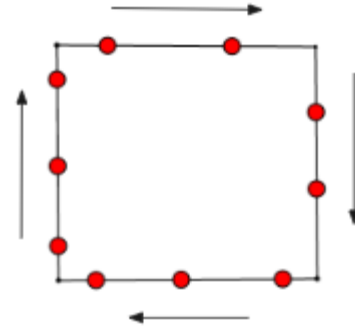
# Next Step: Group Strategies

- Surround and close-in on a target



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- Surround and close-in on a target
- Patrol a perimeter



# Motivation

With enough data generated from implementation of specific tasks, we may train an autonomous model.

# References & Acknowledgements



Special thanks to:

Dr. Jingjin Yu, Mentor

National Science Foundation, funding provided through grant ISS-1734419

Reference:

Yu, J., & LaValle, S.M. (2012). Distance Optimal Formation Control on Graphs with a Tight Convergence Time Guarantee, presented at 51st IEEE Conference on Decision and Control, Maui, HA, December 10-13.